

Some traceability problems in analytical assays of interest in thermal metrology

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**Until 2005: CNR, Istituto di Metrologia "G.Colonnetti" (IMGC), Torino, Italy*

Why worry about **isotopic composition** in thermal metrology?

- Sample-to-sample variations in isotopic composition may contribute to **measurable differences** between standards maintained by the National Metrology Institutes
 - *Compositional variations may result from intrinsic differences in the compositions of natural sources or from fractionation as a result of processing operations*
- The presence of more than one isotope may degrade the quality of standards.
- The isotopic composition must be known with a sufficiently low uncertainty and the analytical assay must give the **absolute composition**, being not the relative one sufficient, since the standards are referring to the thermodynamic state of the substances. Consequently, **the traceability of the chemical assays is a requirement.**

The temperature standard: ITS-90

Fixed Points

- **Physical state**: specified as two or three phase equilibrium
 - Triple Points (TP): H₂, Ne, O₂, Ar, Hg and H₂O
 - Melting Point (MP): Ga
 - Liquid-Vapor Points (VP): ³He, ⁴He and H₂
 - Freezing Points (FP): In, Sn, Zn, Al, Ag, Au, Cu
- **Chemically pure**: unspecified, but generally taken as highest available (the definition is for ideally pure substances –no chemical impurities)
- **Isotopic composition**: loosely specified
 - Uniquely specified in one case only (³He),
 - H₂O TP: “substantially” that of ocean water (*formerly*)
 - all others are specified only as “natural isotopic composition”,
except, from 2005, H₂ (SLAP) and H₂O (VSMOW) .

What is meant by “Natural” Isotopic Composition?

- **Isotopes found in nature generally vary in composition**
- **Natural processes can fractionate elemental isotopes**
 - Not all natural systems are in isotopic equilibrium
- **Terrestrial Abundance may not be uniform or constant**
 - terrestrial ¹ cosmic abundance
- *Handbook values should be treated as terrestrial averages (at best)*
- **Composition depends on the source:**
 - Primordial (Stellar)
 - Terrestrial Atmospheric (e.g. Meteoric, etc.)
- **...And, or the genesis:**
 - Radiogenic (e.g. the stable daughters of radionuclides)
 - Lithogenic (*Nucleogenic*, neutron activation in crustal rocks of U or Th)
 - Cosmogenic
 - Anthropogenic
- **Isotopic fractionation can also occur during industrial processes**

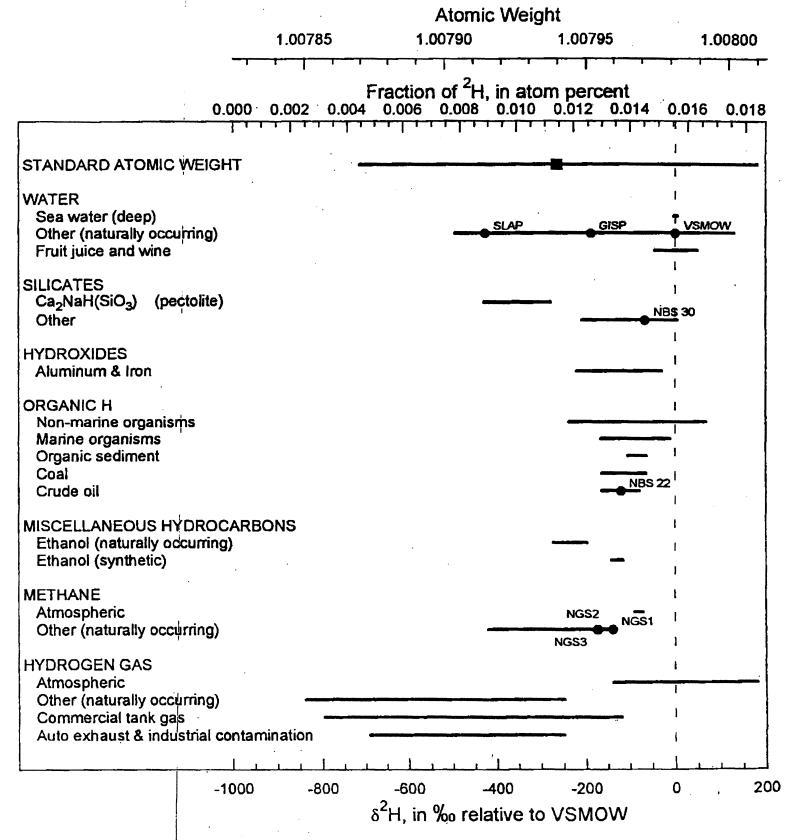
Hydrogen

- **Two Stable Isotopes †**
 - ^1H **99.984426%**
 - ^2H **0.015574%**
- **Terrestrial Inventories**
 - **Oceans**
 - **Continental ground and surface water**
 - **Crustal Rock and Sediments**
 - **Organic Material (e.g. bio-mass, oil, natural gas)**
 - **Atmosphere (only 0.5 ppm at sea level)**
- **Almost all commercial hydrogen gas is synthesized from organic material**
- **Isotopic fractionation effects in gas are very large:**

$$d^2\text{H} = -750 \text{ permil!}$$

† VSMOW, IUPAC, 1997

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Hydrogen natural variability
 after T.Coplen et al., *Pure Appl. Chem.*, Vol. 74,
 No. 10, pp. 1987–2017, 2002.

Equilibrium hydrogen fixed points

• $e\text{-H}_2$ VP₂, (101 kPa) 20.27 K

→ Heavier gases will have lower VP, or higher T at constant P

→ Use ideal solution of H_2 and HD to predict DT at constant P

→ Archival data on P - T of HD from NBS, Hoge and Arnold, 1951

→ Condensation and Evaporation Lines (vapor/liquid ratio dependence)

• $e\text{-H}_2$ VP₁, (33 kPa) 17.03 K

→ Same as above

• $e\text{-H}_2$ TP, 13.8033 K

→ Heavier gases will have higher melting temperatures

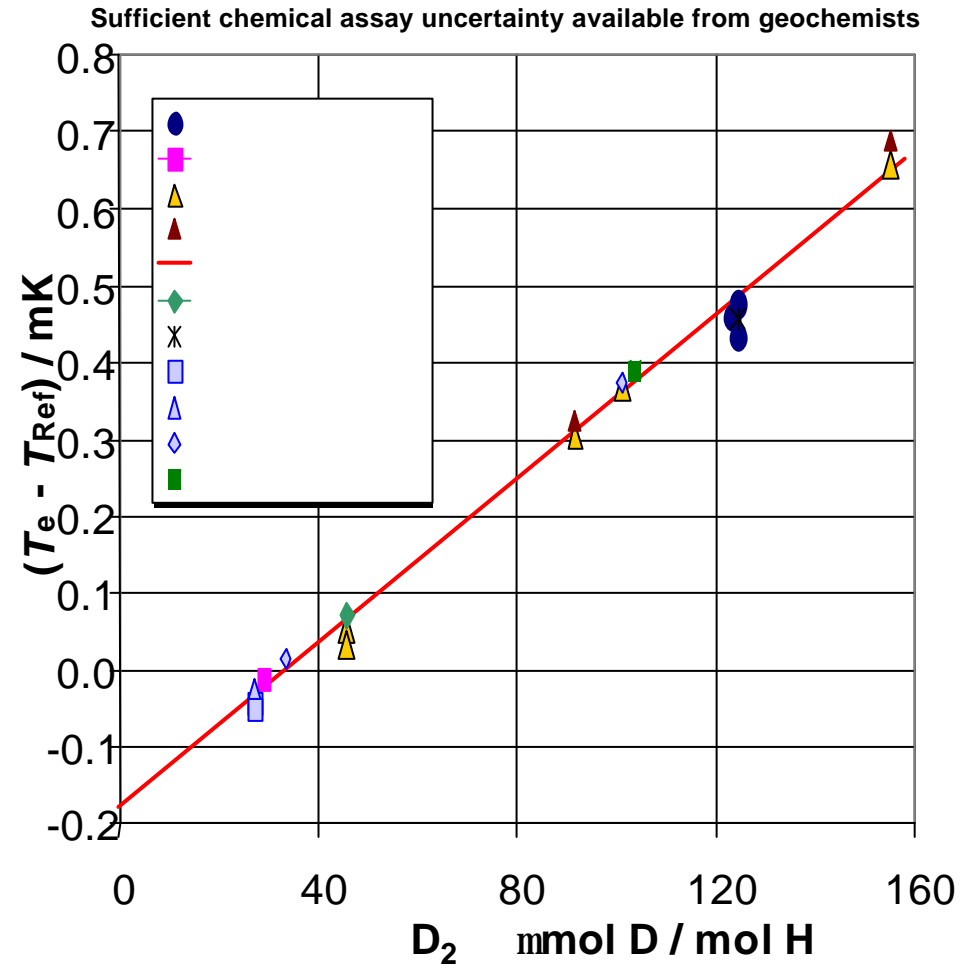
→ Archival Data on melting $p\text{-H}_2$ +HD: Bereznyak, *et. al.*, *Soviet JETP*, 1970.

→ 2.8 mK/(mmol HD/mol H_2) ® ~ 1.0 mK ambiguity for natural compositions

→ ~ 600 mK uncertainty ambiguity from commercial tank gas

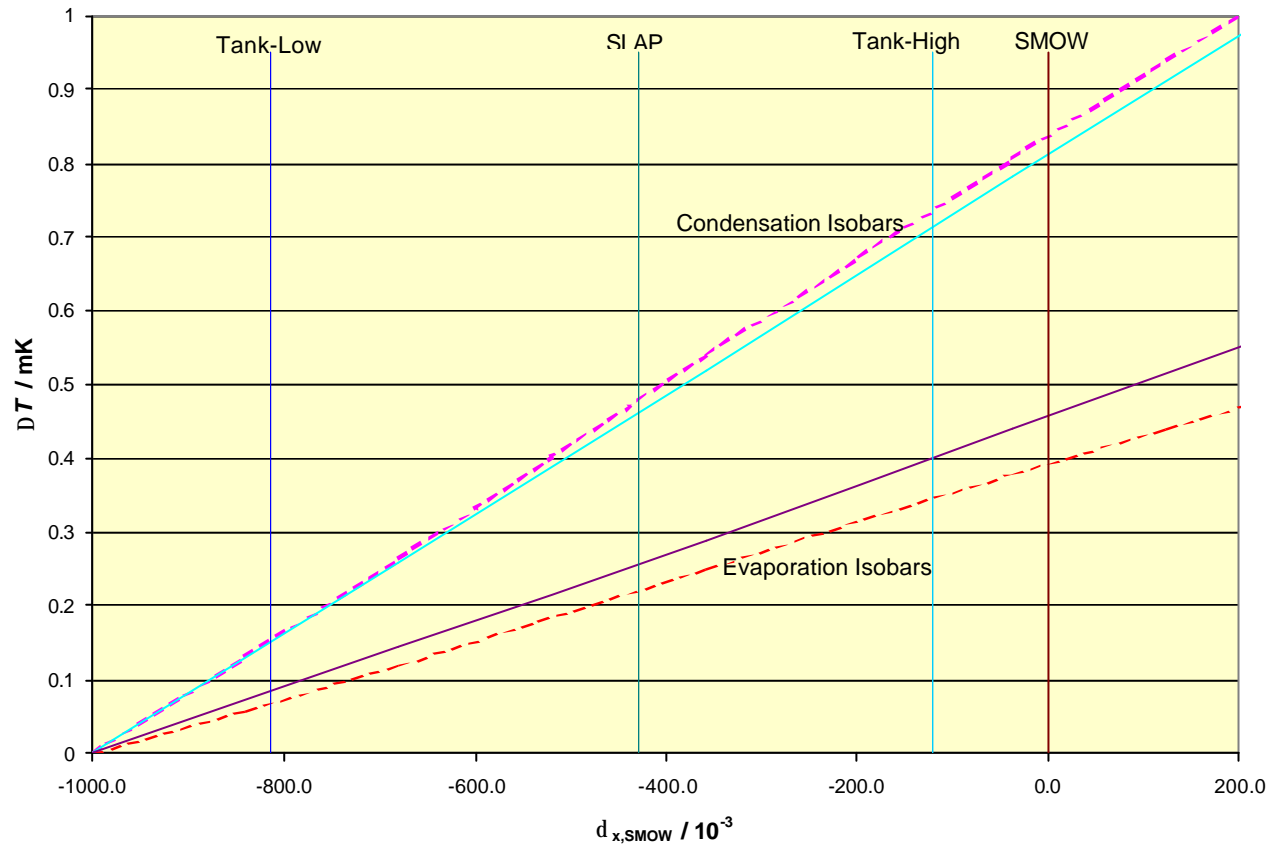
→ Total range observed in recent studies: ~ 700 mK (aimed 20 mK)

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Slope: (5,4₂ ± 0,3₁) mK per mmol D/mol H
(Fellmuth *et al.*, *Metrologia* 2005)

Liquid-vapour equilibria in hydrogen isotope mixtures



Calculated elevation in the 33 kPa (dashed lines) and 101 kPa (solid lines) isobars for condensation and evaporation in the dilute limit of an ideal e-H₂ + HD solution. The compositions of SLAP and VSMOW are shown along with the range of reported tank gas compositions. (Tew, 2001)

Terrestrial origins of neon

- **Three stable isotopes of neon†**
 - ^{20}Ne **90.4838%** **Primordial**
 - ^{21}Ne **0.2696%** **Prim.+ Nucleogenic $^{18}\text{O}(\alpha, n)^{21}\text{Ne}$**
 - ^{22}Ne **9.2465%** **Prim.+ Nucleogenic $^{25}\text{Mg}(n, \alpha)^{22}\text{Ne}$**
- **Bulk of terrestrial inventory is atmospheric**
 - 18.2 ppm concentration
 - much lower than cosmic abundance
- **Most commercial neon is extracted from air, but not all**
- **Natural gas wells rich in He contain trace amounts (1 to 2 ppm) Ne**
 - **neon from NG is enriched in nucleogenic isotopes, ^{21}Ne and ^{22}Ne**
 - neon becomes concentrated in helium as byproduct of separation
 - economics of He supply and demand could influence the source of commercial neon gas

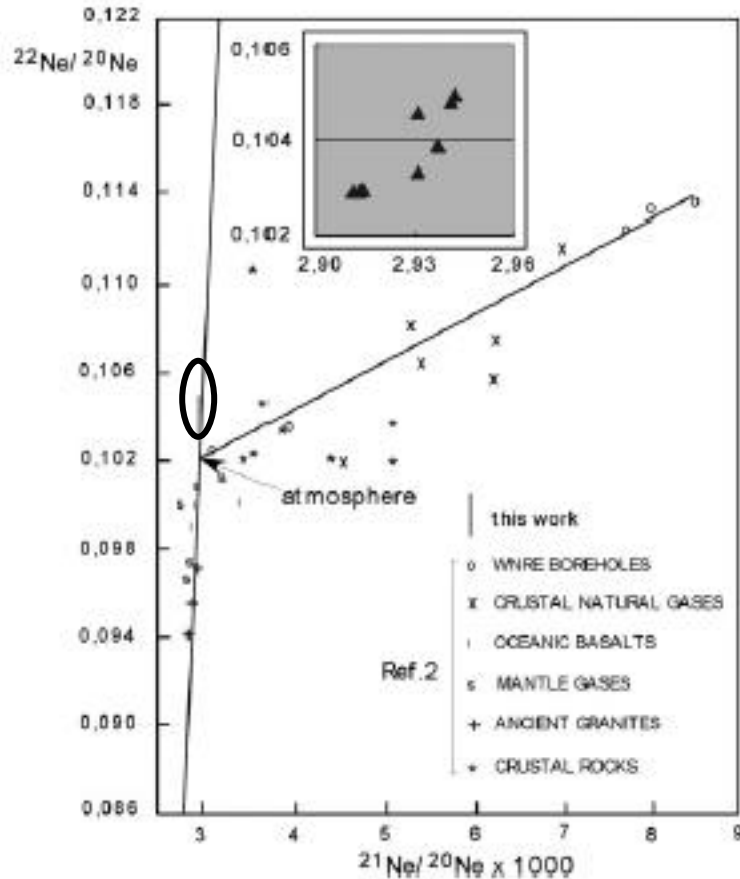
† Air, IUPAC, 1997

Triple Point of Neon

- $T_{90}(\text{natNe TP}) = 24.5561 \text{ K}$ (defined for “natural” isotopic composition)
- **Isotopic measurements, Furukawa, NBS, 1972**
 - $T(^{20}\text{Ne TP}) - T(\text{natNe TP}) = - 13 \text{ mK}$
 - $T(^{22}\text{Ne TP}) - T(\text{natNe TP}) = +134 \text{ mK}$
 - In that case, “Natural” means Ne as derived from air separation
 - Sensitivity to variations in ^{22}Ne are 1.5 mK/atom %
- **For Ne gas derived from natural gas (helium separation)**
 - Keyes, OK (panhandle): ^{20}Ne 89.69%; ^{21}Ne 0.646%; ^{22}Ne 9.66%,
 - $T(\text{NGNe}) - T(\text{natNe TP}) = + 900 \text{ mK}$ (estimated) **(aimed: 20 mK)**

Triple Point of Neon

Sufficient chemical assay uncertainty available only from IRMM, Geel.



Sample #	$n(^{21}\text{Ne}) / n(^{20}\text{Ne})$	$\Delta T_{\text{tp}} / \mu\text{K}$	$n(^{22}\text{Ne}) / n(^{20}\text{Ne})$	$\Delta T_{\text{tp}} / \mu\text{K}$
7	-0,000069	-5	0,000700	103
5	-0,000043	-3	0,001610	237
1	-0,000049	-3	0,001090	160
7	-0,000066	-5	0,000710	104
3	-0,000049	-3	0,002360	347
4	-0,000043	-3	0,001670	245
2	-0,000038	-3	0,002730	401
6	-0,000039	-3	0,002600	382
7	-0,000067	-5	0,000710	104

2003 data: deviations from “natural isotopic composition” (IUPAC, 1997) of the measured composition values and the corresponding effect on DT_{tp} .

(after Pavese et al., Analytical Chemistry 2005)

Oxygen

- **Three stable isotopes of oxygen†**
 - ^{16}O **99.7628%**
 - ^{17}O **0.0372%**
 - ^{18}O **0.20004%**
- **Terrestrial Inventories**
 - **Crust - isotopically varied, usually enriched ^{18}O :**
 - Silicates: $d^{18}\text{O}_{\text{VSMOW}} = +5$ to $+28$ per mil
 - Nitrates: $d^{18}\text{O}_{\text{VSMOW}} = -10$ to $+80$ per mil
 - **Atmosphere - isotopically very uniform, enriched ^{18}O : $d^{18}\text{O}_{\text{VSMOW}} = 23.5$ per mil**
 - **Oceans - isotopically uniform in temperate zones**
- **Laboratory Oxygen**
 - **bulk gas cryogenically separated from air**
 - **prepared gas derived from thermal decomposition of manganates or chlorates**
- **No temperature measurements at known isotopic composition available**
- **Estimated effect on T_{tp} (*Gonfiantini, priv.comm.*): **20 mK for a 4% variability****

† VSMOW, IUPAC, 1997

Argon

- **Three stable isotopes of argon †**

→³⁶Ar **0.337 (3)%**

→³⁸Ar **0.063 (1)%**

→⁴⁰Ar **99.600 (3)%**

- **$(^{40}T_{\text{tp}} - ^{36}T_{\text{tp}}) = 59 \text{ mK}$, experimental**

- **Effect on T_{tp} for a variability equal to IUPAC uncertainty on ⁴⁰Ar : 1.5 mK**

† VSMOW, IUPAC, 1997

Geochemistry of water

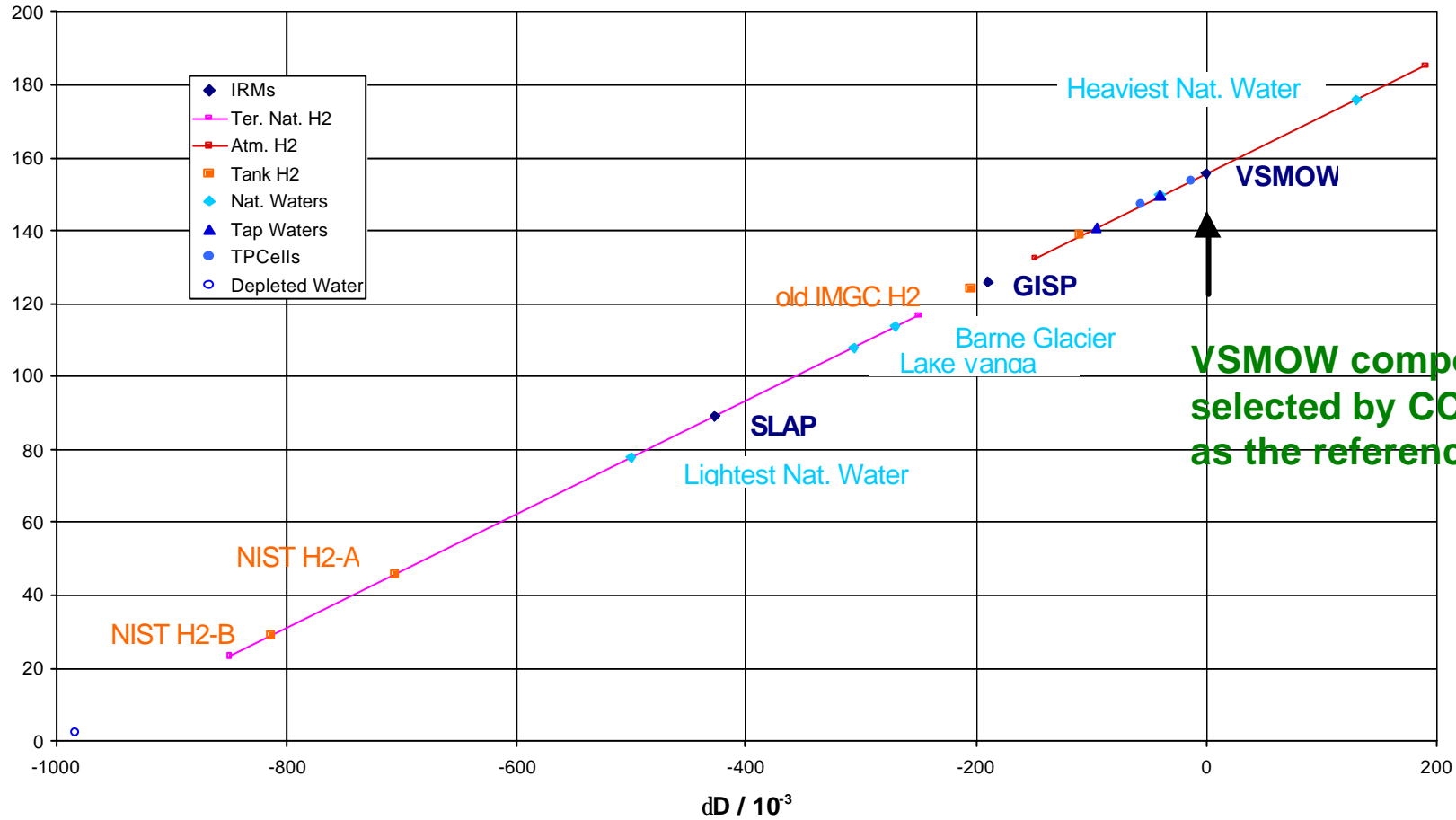
- Natural water is a mixture of four different isotopic components:
 - $^1\text{H}^{16}\text{O}^1\text{H}$
 - $^2\text{H}^{16}\text{O}^1\text{H}$
 - $^1\text{H}^{17}\text{O}^1\text{H}$
 - $^1\text{H}^{18}\text{O}^1\text{H}$
 - + other very small concentrations of second order combinations
- **Heavier isotopes are depleted in polar waters**
- **Relative depletion is correlated in precipitation: $d^2\text{H} = 8 \cdot d^{18}\text{O} + 10$**
- **SLAP vs. SMOW:**
 - $^2\text{H}/^1\text{H} = 155.74 \cdot 10^{-6}$ in SMOW
 - $^2\text{H}/^1\text{H} = 89.02 \cdot 10^{-6}$ in SLAP
 - $^{18}\text{O}/^{16}\text{O} = 2.0051 \cdot 10^{-3}$ in SMOW
 - $^{18}\text{O}/^{16}\text{O} = 1.8938 \cdot 10^{-3}$ in SLAP

$$d^2\text{H}_{\text{VSMOW}} = -428 \text{ per mil}$$

$$d^{18}\text{O}_{\text{VSMOW}} = -55.5 \text{ per mil}$$

D/H content in molecular hydrogen and water

Isotopic content of hydrogen and water samp



VSMOW composition selected by CCT as the reference (2005)

Triple point of water – 1

- **Triple Point of Water (TPW) definition of the SI Kelvin**
 - Adopted by the CCT in 1954
 - definition does not refer to ocean water or any isotopic composition
- **TPW cells**
 - are almost always derived from continental (fresh) surface water
 - temperate latitudes
- **ITS-90**
 - specifies an isotopic composition “substantially” that of ocean water
- **Natural water variations affect on TPW (aimed 10–20 mK)**
 - 200 mK typical between polar fresh and polar sea ice
 - 30 mK to 50 mK between temperate continental and ocean water
 - 250 mK (estimated) between SLAP and SMOW

Triple point of water – 2

Laboratory	Date	96/2-96/1 /mK	96/3-96/1 /mK	96/4-96/1 /mK	98/1-96/1 /mK	std. dev. /mK
MSL	Sept. 96	-0.156	-0.178	0.038		0.013
NIST	May 97	-0.150	-0.172	0.020		0.012
MSL	Apr. 98				-0.989	0.040
NPL	Aug. 98	-0.116	-0.154	0.034		0.034
NIST	Nov. 98				-0.960	0.014
NPL	June 00	-0.139	-0.155		-0.988	0.040
MSL	Apr. 02	-0.135	-0.151	0.051	-0.963	0.014
mean	DT	-0.145	-0.165	0.034	-0.964	
sm		0.007	0.005	0.006	0.008	

(After *D R White, T D Dransfield, G F Strouse, W L Tew, R L Rusby, J Gray, TMCSI 8, ISA, New York, 2003.*)

If Kiyosawa's correction values are adopted, the uncertainty in the isotope corrections for typical cells is almost certainly within 10 μK , may be within 1 μK .

Metal fixed points

Fixed Point	$T_{90} / ^\circ\text{C}$	Isotopes	Fixed Point	$T_{90} / ^\circ\text{C}$	Isotopes
Hg	-38.8344	7	(Al	660.323	1)
Ga	29.7646	2	Ag	961.78	2
In	156.5985	2	(Au	1064.18	1)
Sn	231.928	10	Cu	1084.62	2
Zn	419.527	5			

No $T - x$ data presently available sufficient for thermal metrology

Why worry about **chemical impurities** in thermal metrology?

Table 1. The fixed points of the ITS-90, including the latent heats of fusion (L), the first cryoscopic constants (A), the best available purities for the various substances as stated by their commercial sources, the uncertainty (strictly speaking, the freezing point depression predicted on the basis of the first cryoscopic constant) resulting from this less-than-ideal purity, and a desirable (if somewhat arbitrary) target uncertainty for the impurity component.

Substance	T_{90} (K)	L (kJ mol ⁻¹)	A (K ⁻¹)	Available nominal purity $\times 100$	Predicted uncertainty (mK)	Target uncertainty (mK)	Target impurity $\times 10^6$
e-H ₂	13.8033	0.117	0.073 9	99.999 9	0.014	0.04	3.0
Ne	24.5561	0.335	0.066 8	99.999	0.150	0.04	2.7
O ₂	54.3584	0.444	0.018 1	99.999 9	0.055	0.04	0.7
Ar	83.8058	1.188	0.020 3	99.999 9	0.049	0.04	0.8
Hg	234.3156	2.292	0.005 02	99.999 999	0.002	0.04	0.2
H ₂ O	273.16	6.008	0.009 68	99.999 999	0.001	0.01	0.1
Ga	302.9146	5.585	0.007 32	99.999 99	0.014	0.04	0.3
In	429.7485	3.264	0.002 13	99.999 99	0.047	0.1	0.2
Sn	505.078	6.987	0.003 29	99.999 9	0.304	0.1	0.3
Zn	692.677	7.385	0.001 85	99.999 99	0.054	0.1	0.2
Al	933.473	10.79	0.001 49	99.999 95	0.336	0.5	0.7
Ag	1234.93	11.3	0.000 891	99.999 9	1.122	1	0.9
Au	1337.33	12.364	0.000 831	99.999 9	1.203	1	0.8
Cu	1357.77	13.14	0.000 857	99.999 9	1.167	1	0.9

(After *K D Hill and S Rudtsch, Metrologia 42 (2005) L1-L4*)

**Individual chemical impurities critically affect some of the temperature standards.
Reliable and traceable assays are needed for low-concentrations.**